

# Safe Exploration and Optimization of Constrained MDPs using Gaussian Processes

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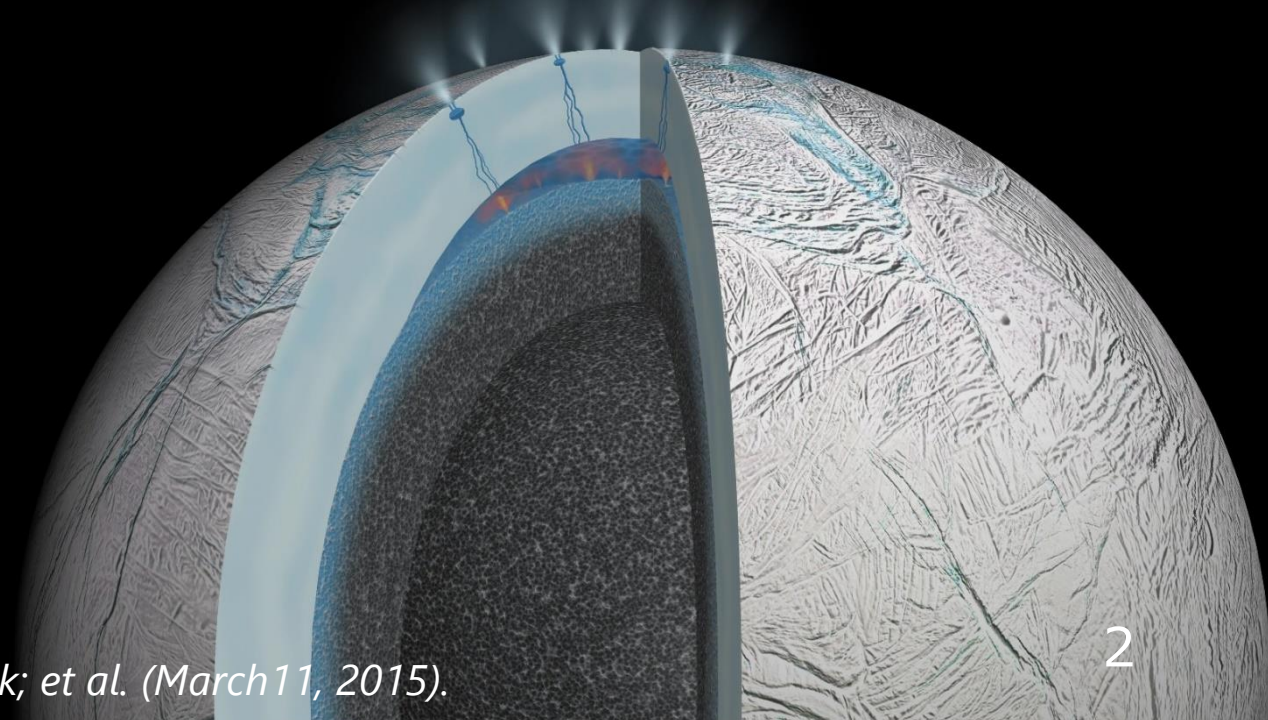
AAAI Conference on Artificial Intelligence



# Background

There is increasing need for automated exploration of the *unknown* environment

- *Unknown where is dangerous/safe*
- *Unknown where is scientifically worthwhile to visit*



# Problem Statement

We would like an agent to:

- Obtain scientifically valuable data
- Guarantee safety



## Problem formulation

$$\max \sum_{k=1}^N \gamma^{k-1} f_k(\mathbf{x}_k)$$

$$\text{subject to } g_k(\mathbf{x}_k) > h \quad \forall k = [1 \ N - 1]$$

$\mathbf{x}_k$  : state vector

$N$  : terminal time step

$f_k(\mathbf{x}_k)$  : reward function

$g_k(\mathbf{x}_k)$  : safety function

$h$  : safety threshold

$\gamma$  : discount rate

We assume that reward and safety are a priori unknown.

# Our Contributions

## Reinforcement learning

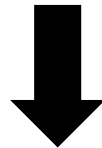
[Sutton and Barto, 1998;  
Bertsekas and Tsitsikils, 1995]

$$\max \sum_{k=1}^N \gamma^{k-1} f_k(\mathbf{x}_k)$$

## Risk-Sensitive Decision Making

[Schwarm and Nikolaou, 1999;  
Blackmore et al., 2010]

Add risk-sensitivity  
(Safety constraint)



Assume that safety  
is a priori unknown

## Our research

$$\max \sum_{k=1}^N \gamma^{k-1} f_k(\mathbf{x}_k)$$

subject to  $g_k(\mathbf{x}_k) > h \quad \forall k = [1 \ N - 1]$

# Exploration & Exploitation

If you were a treasure hunter, what would you do?

- Collect treasure which has been already identified?
- Seek more valuable treasure?
- Try to search safe region ?



Such a problem is called *exploration/exploitation problem*

# Three-way trade-off

Check where is safe/dangerous



# How should we deal with safety?

It is difficult to guarantee safety because ...



It is too late to realize the hazard after hitting it!  
Just single mistake may result in failure.

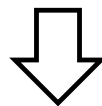
We must predict hazards before actually visiting unsafe states.

# How should we deal with safety?

Parameters in natural environments have some regularity



We assume that **similar states** have **similar values of safety function**.

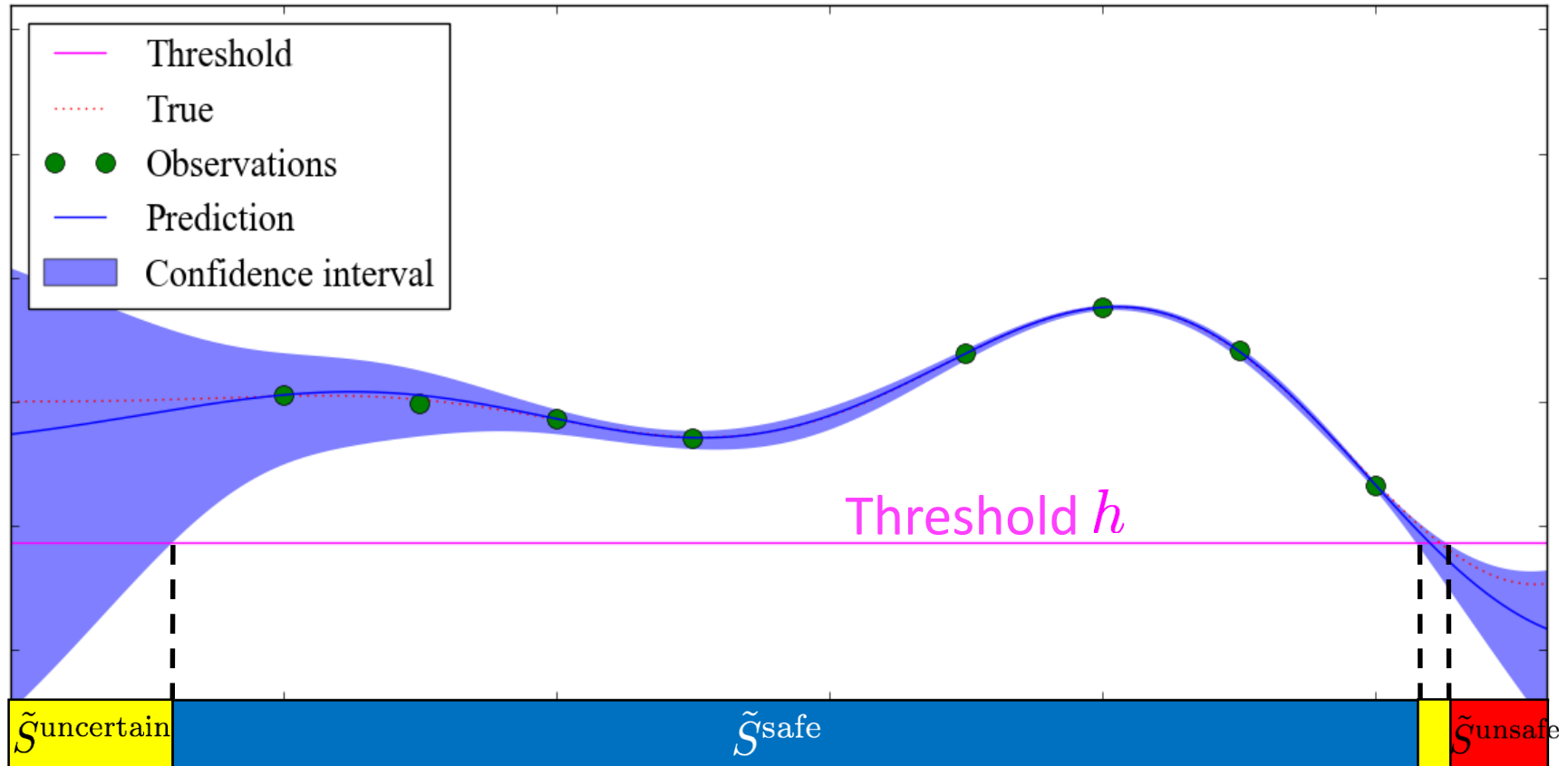


Evaluate safety function using **Gaussian Processes (GPs)**



# Gaussian Processes

Safety constraint:  $g_k(x_k) \geq h$



An agent can guarantee safety with high probability.  
(For more detail, see our paper.)

# Exploration/Exploitation Problem

Exploration  
of safety

M. Turchetta et al. (2016)  
focuses on exploration of  
safety.



Key point

How can we balance  
the three objectives?

Exploitation  
of reward

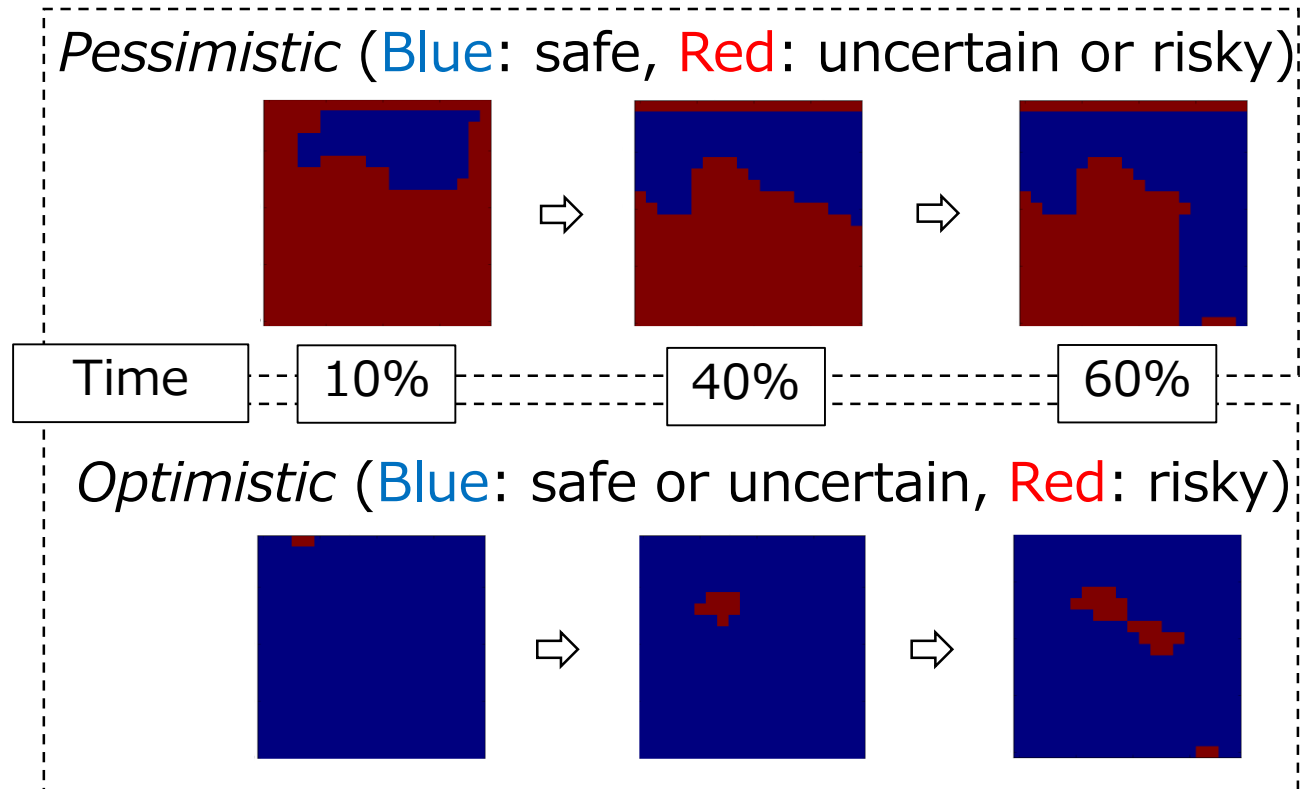
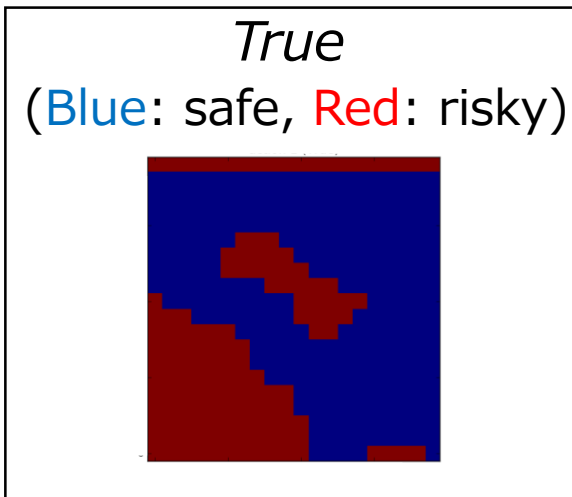


Exploration  
of reward

A great deal of previous work  
in the field of reinforcement learning  
has worked on this problem

# Classification of State Space

- Classify the state space into three regions using GP  
→ *safe space, uncertain space, risky space*

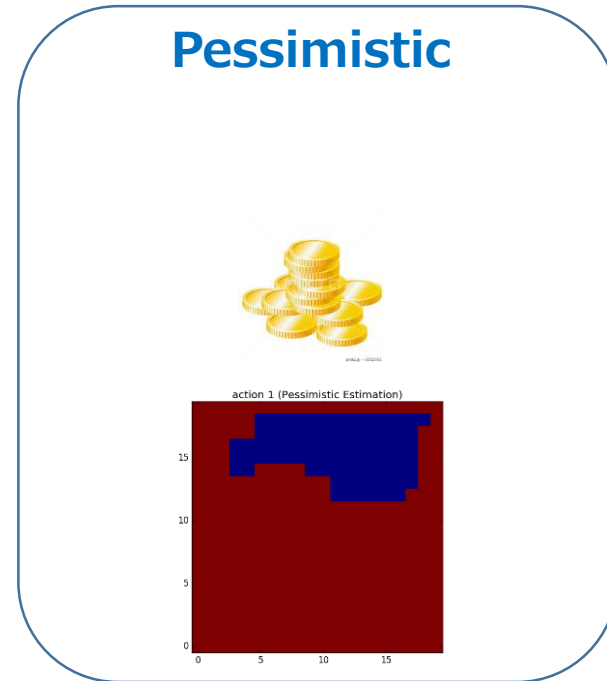
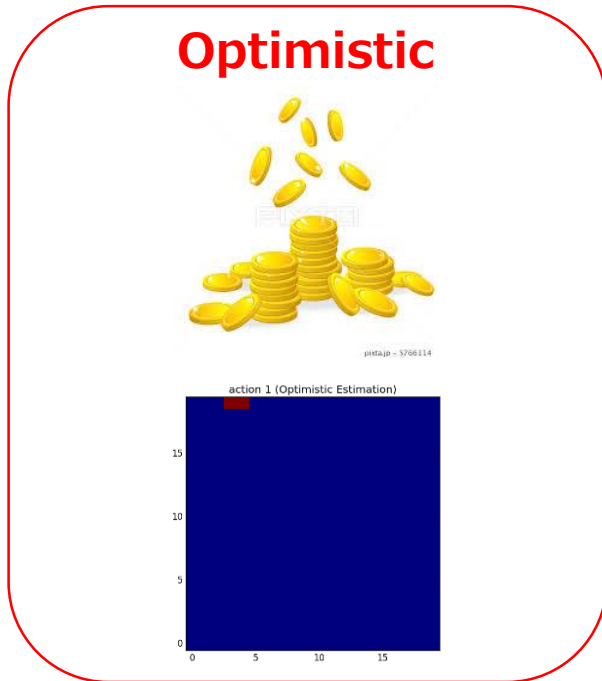


# Introduction of Delta-J

Difference of cumulative reward for **Optimistic** and **Pessimistic** cases means **the need for exploration of safety**

$$\Delta J(s) = \hat{J}(s) - \bar{J}(s)$$

**Optimistic**   **Pessimistic**



Difference is big  $\rightarrow$  *“exploration of safety” is necessary*  
Difference is small  $\rightarrow$  *it is OK to focus on reward*

# Overall Policy

exploration/exploitation  
of reward

exploration  
of safety

$$\pi_N(s, b^f, b^g) = \arg \max_{s \in S^{\text{safe}}} \{ \bar{J}(s, b^f, b^g) + \lambda \Delta J(s, b^f, b^g) \}$$

↓

$0 \leq \lambda \leq 1$

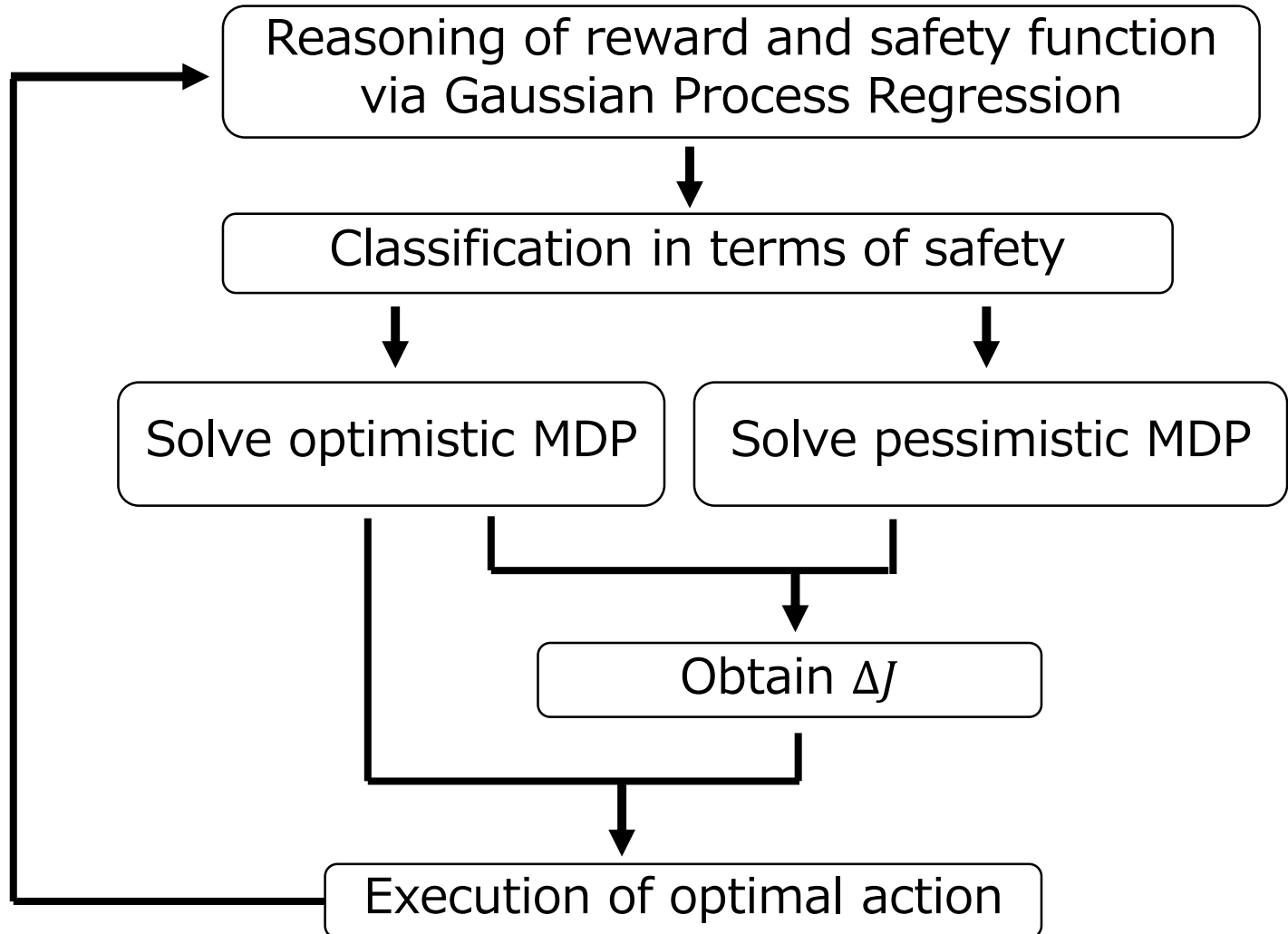
value function for  
*Optimistic case*

value function for  
*Pessimistic case*

$$\pi_N(s, b^f, b^g) = \arg \max_{s \in S^{\text{safe}}} \{ \lambda \hat{J}(s, b^f, b^g) + (1 - \lambda) \bar{J}(s, b^f, b^g) \}$$

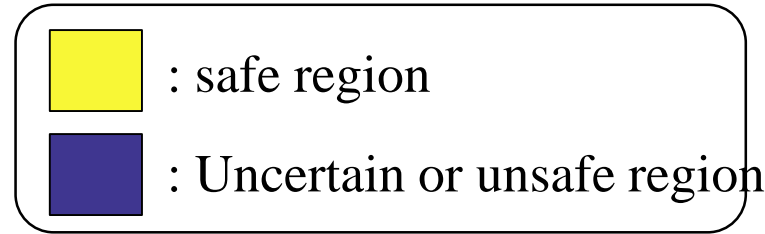
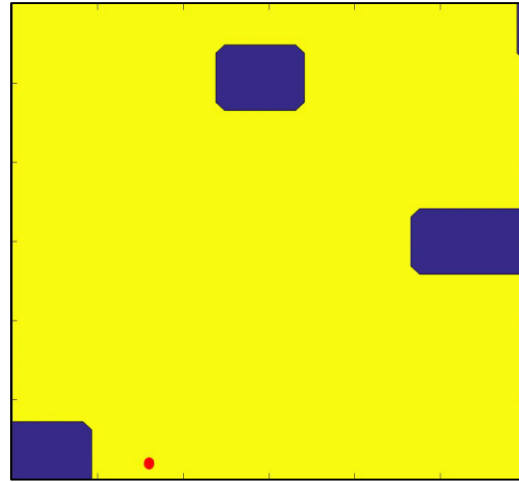
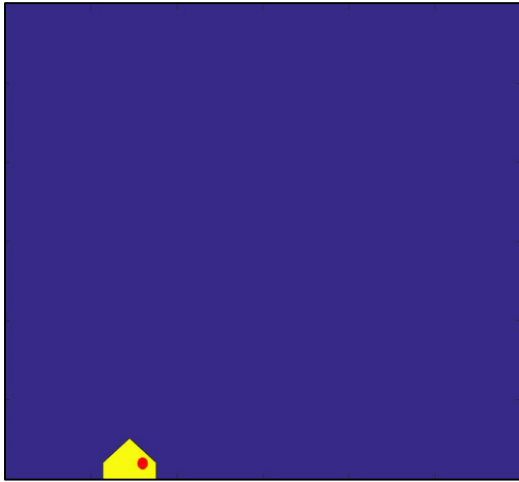
An agent should choose a state with the maximum value of the dividing point of **optimistic** and **pessimistic** cases.

# Algorithm flow

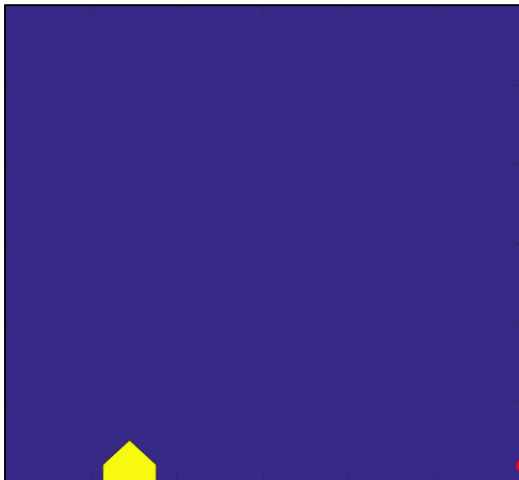


# Simulation result

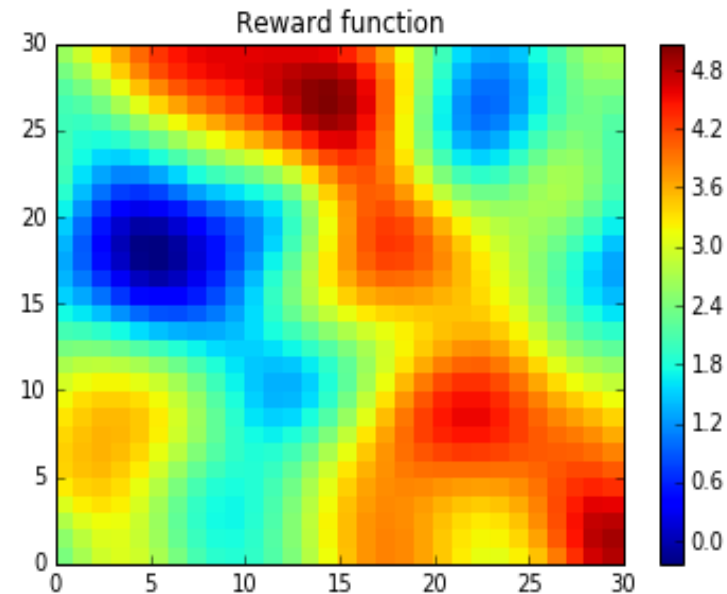
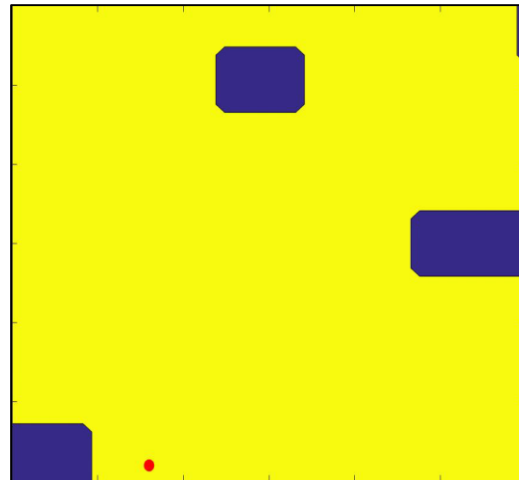
Proposed method    Safety/reward known



M. Turchetta et al.



Safety known



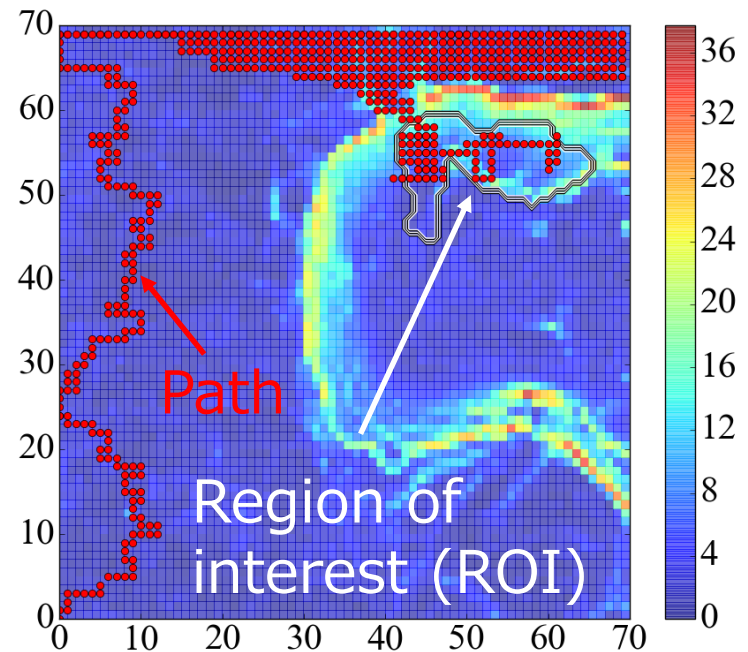
# Mars Surface Exploration Example

Conducted a simulation using Mars terrain data based on real Mars surface exploration scenario.

- Safety function: slope angle
- Threshold: 25deg
- Reward function: binary (one within in ROI)

## Result

- Succeeded in arriving at ROI while guaranteeing safety.
- Proved that our proposed method can be applied to practical applications





# Conclusion

1. Formulate a problem in which a MDP is safely explored and optimized with a priori unknown reward and safety
2. Propose an algorithm to balance exploration of reward, exploitation of reward, and exploration of safety
3. Demonstrate the effectiveness of our proposed method by the three types of simulation including one using real Martian data